



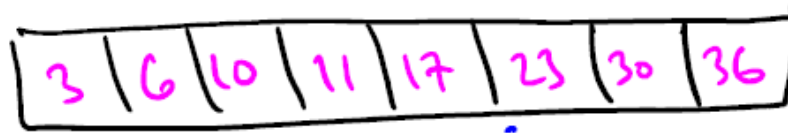
# Data Structures

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Balanced Search  
Trees: Supported  
Operations



# Sorted Arrays: Supported Operations



## OPERATIONS

SEARCH

SELECT (given order statistic  $l$ )

MIN/MAX

PRED/SUCC (given pointer to a key)

RANK (i.e., # of keys less than or equal to  
a given value)

OUTPUT IN SORTED ORDER

*BUT WHAT ABOUT  
INSERTIONS + DELETIONS?  
(would take  $\theta(n)$  time)*

## RUNNING TIME

$\theta(\log(n))$

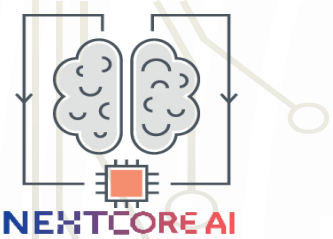
$O(1)$

$O(1)$

$O(1)$

$O(\log(n))$

$O(n)$



# Balanced Search Trees: Supported Operations

Raison d'être : like sorted array + fast (logarithmic) inserts + deletes !

## OPERATIONS

SEARCH  
SELECT  
MIN/MAX  
PRED/SUCC  
RANK  
OUTPUT IN SORTED ORDER  
INSERT  
DELETE

## RUNNING TIME

Also supported by hash tables

Also supported by heaps

$\theta(\log(n))$   
 $O(\log(n))$   
 $O(\log(n))$   
 $O(\log(n))$   
 $O(\log(n))$   
 $O(n)$   
 $O(\log(n))$   
 $O(\log(n))$

Up from  $O(1)$

new